

Name _____ Date _____ Period _____

Pre-Calculus Unit 2 Practice Test—Answers

1. Solve $4(x - 3)^2 + 5 = -25$ using the square root method.

$$\begin{aligned} 4(x - 3)^2 &= -30 \\ (x - 3)^2 &= -\frac{30}{4} \\ x - 3 &= \pm \sqrt{-\frac{30}{4}} \end{aligned} \qquad \begin{aligned} x - 3 &= \pm \frac{\sqrt{30}}{2} i \\ x &= 3 \pm \frac{\sqrt{30}}{2} i \end{aligned}$$

2. Solve $8x^2 - 14x = 15$ by factoring.

$$\begin{aligned} 8x^2 - 14x - 15 &= 0 \\ 8x^2 - 20x + 6x - 15 &= 0 \\ 4x(2x - 5) + 3(2x - 5) &= 0 \\ (2x - 5)(4x + 3) &= 0 \\ x = \frac{5}{2} \text{ and } x = -\frac{3}{4} \end{aligned}$$

3. Solve $x^2 - 6x + 4 = 0$ by completing the square.

$$\begin{aligned} x^2 - 6x &= -4 \\ (x - 3)^2 &= -4 + (3)^2 \\ (x - 3)^2 &= -4 + 9 \\ (x - 3)^2 &= 5 \\ x - 3 &= \pm\sqrt{5} \\ x &= 3 \pm \sqrt{5} \end{aligned}$$

4. Solve $2x^2 - 3x + 5$ using the quadratic formula.

$$\frac{3 \pm \sqrt{(-3)^2 - 4(2)(5)}}{2(2)} = \frac{3 \pm \sqrt{-31}}{4} = \frac{3 \pm i\sqrt{31}}{4}$$

5. Find the exact solution using any method $6x^2 + 2x + 3 = 1$.

$$6x^2 + 2x + 2 = 0$$

$$\frac{-2 \pm \sqrt{(2)^2 - 4(6)(2)}}{2(6)} = \frac{-2 \pm \sqrt{-44}}{12} = \frac{-2 \pm 2i\sqrt{11}}{12} = \frac{-1 \pm i\sqrt{11}}{6}$$

6. What is the fundamental theorem of Algebra?

For a polynomial of degree n there are n real zeros.

7. Use your calculator to find the approximate solutions to the equation $2x^4 - 3x^3 + 2 = 0$.

There are no real zeros because it doesn't cross the x -axis.

Are there any complex solutions to this equation (you don't need to find them if there are)? If so, how many? Explain how you know.

There are 4 complex solutions because there are no real zeros and it is a 4th degree polynomial.

Solve the equations. You may use your calculator (to start), synthetic division, factoring, or the quadratic formula. Leave answers as exact answers in simplified form.

8. $x^4 - 4x^2 + 3 = 0$

$$\begin{array}{r|rrrrr} 1 & 1 & 0 & -4 & 0 & 3 \\ & & 1 & 1 & -3 & -3 \\ \hline -1 & 1 & 1 & -3 & -3 & 0 \\ & & -1 & 0 & 3 & \\ \hline & 1 & 0 & -3 & 0 & \\ \hline \end{array}$$

$x^2 - 3 = 0$
 $x^2 = 3$

$$x^2 = 3$$

$$x = \pm\sqrt{3}$$

$$\text{Zeros: } -1, 1, \sqrt{3}, -\sqrt{3}$$

9. $x^4 - 81 = 0$

$$\begin{array}{r|rrrrr} 3 & 1 & 0 & 0 & 0 & -81 \\ & & 3 & 9 & 27 & 81 \\ \hline -3 & 1 & 3 & 9 & 27 & 0 \\ & & -3 & 0 & -27 & \\ \hline & 1 & 0 & 9 & 0 & \\ \hline \end{array}$$

$x^2 + 9 = 0$
 $x^2 = -9$

$$x^2 = -9$$

$$x = \pm 3i$$

$$\text{Zeros: } -3, 3, 3i, -3i$$

10. $x^4 + 5x^3 + x^2 + 5x = 0$

$$\begin{array}{r|rrrrr} -5 & 1 & 5 & 1 & 5 & 0 \\ & & -5 & 0 & -5 & 0 \\ \hline 0 & 1 & 0 & 1 & 0 & 0 \\ & & 0 & 0 & 0 & \\ \hline & 1 & 0 & 1 & 0 & \\ \hline \end{array}$$

$x^2 + 1 = 0$
 $x^2 = -1$

$$x^2 = -1$$

$$x = \pm i$$

$$\text{Zeros: } -5, 0, i, -i$$

No Calculator Section

11. State the degree, number of possible real zeros, and turning points of the function. Then determine all of the real zeros by factoring.

$$f(x) = 2x^2 - 5x - 3$$

Degree: 2

Possible real zeros: 2

Possible turning points: 1

$$2x^2 - 5x - 3 = 0$$

$$2x^2 - 6x + x - 3 = 0$$

$$2x(x - 3) + 1(x - 3) = 0$$

$$(x - 3)(2x + 1) = 0$$

$$x = 3 \text{ and } x = -\frac{1}{2}$$

12. Write the function $f(x) = 3x^4 + 11x^2 - 4$ in completely factored form.

$$\begin{aligned} &3x^4 + 12x^2 - x^2 - 4 \\ &3x^2(x^2 + 4) - 1(x^2 + 4) \\ &(x^2 + 4)(3x^2 - 1) \end{aligned}$$

13. Sketch a complete graph of the function $f(x)$ in #11. List the coordinates of the y-intercept and zeros.

$$\text{x-intercepts: } (x^2 + 4)(3x^2 - 1) = 0$$

$$x^2 + 4 = 0$$

$$x^2 = -4$$

$$x = \pm 2i$$

$$3x^2 - 1 = 0$$

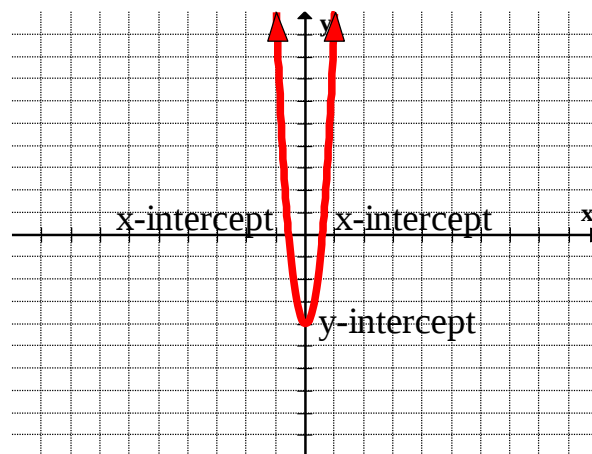
$$3x^2 = 1$$

$$x^2 = \frac{1}{3}$$

$$x = \pm \sqrt{\frac{1}{3}}$$

$$\begin{aligned} \text{y-intercept: } &(0^2 + 4)(3(0)^2 - 1) \\ &(4)(-1) = -4 \end{aligned}$$

$$\text{zeros: } \pm \sqrt{\frac{1}{3}}$$



14. Solve the following inequality.

$$2x^2 + x - 10 < 5$$

$$2x^2 + x - 15 < 0$$

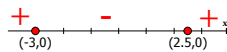
$$2x^2 + 6x - 5x - 15 < 0$$

$$2x(x + 3) - 5(x + 3) < 0$$

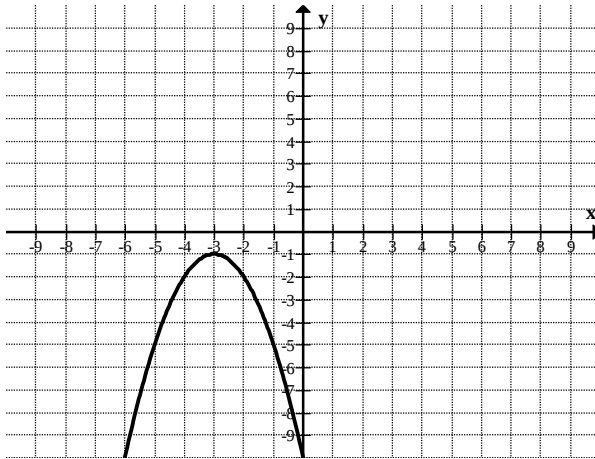
$$(x + 3)(2x - 5) < 0$$

$$x = -3 \text{ and } x = 2.5$$

$$\text{Solution: } (-3, 2.5)$$



15. Write a function for the graph below in vertex form and standard form.



$$y = -(x + 3)^2 - 1$$

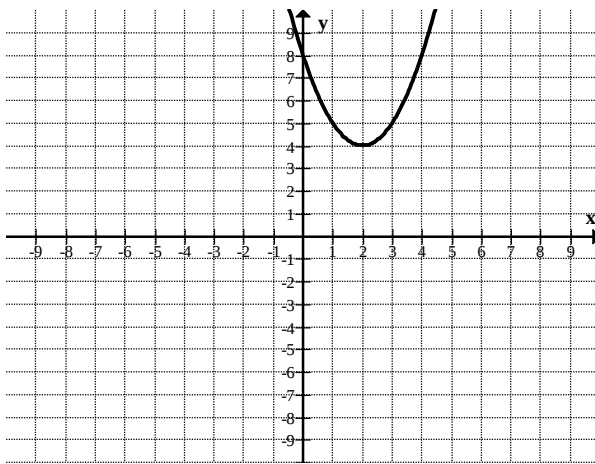
$$y = -(x + 3)(x + 3) - 1$$

$$y = -(x^2 + 6x + 9) - 1$$

$$y = -x^2 - 6x - 9 - 1$$

$$y = -x^2 - 6x - 10$$

16. Write a function for the graph below in vertex form and standard form.



$$y = (x - 2)^2 + 4$$

$$y = (x - 2)(x - 2) + 4$$

$$y = x^2 - 4x + 4 + 4$$

$$y = x^2 - 4x + 8$$

17. Write $f(x) = x^2 + 2x - 3$ in vertex form. Identify the vertex of $f(x)$, the max/min value, and the axis of symmetry.

$$-\frac{2}{2(1)} = -1$$

$$f(-1) = 1 - 2 - 3 = -4$$

$$f(x) = (x + 1)^2 - 4$$

Vertex: $(-1, -4)$ **Min @** $(-1, -4)$

Axis: $x = -1$

18. Write $f(x) = -x^2 - x + 6.5$ in vertex form. Identify the vertex of $f(x)$, the max/min value, and the axis of symmetry.

$$\frac{1}{2(-1)} = -\frac{1}{2}$$

$$f\left(-\frac{1}{2}\right) = -\left(-\frac{1}{2}\right)^2 + \frac{1}{2} + 6.5$$

$$-\frac{1}{4} + \frac{1}{2} + 6.5$$

$$-.25 + .5 + 6.5$$

$$-.25 + 7 = 6.75$$

$$f(x) = -\left(x + \frac{1}{2}\right)^2 + 6.75$$

Vertex: $\left(-\frac{1}{2}, 6.75\right)$

Max @ $\left(-\frac{1}{2}, 6.75\right)$

Axis: $x = -\frac{1}{2}$